

Find intersection of : SECTION 2.3

$$x - y = 3 \quad \text{and} \quad y = x^2 + 5x + 1$$

$$x = 3 + y$$

$$x = 3 - 5 = -2$$

$$y = (3+y)^2 + 5(3+y) + 1$$

$$y = 9 + 6y + y^2 + 15 + 5y + 1 \quad \text{solution } (-2, -5)$$

$$y^2 + 10y + 25 = 0$$

$$(y + 5)(y + 5) = 0$$

$$y = -5$$

p.58, 59

Section 2.4

Q1 Find the values of 2 consecutive numbers,

p.59 the sum of their squares is 61.

x = one no.

y = other no.

$$x = y + 1$$

$$x^2 + y^2 = 61$$

$$(y+1)^2 + y^2 = 61$$

$$x = 5 + 1 = 6$$

$$y^2 + 2y + 1 + y^2 = 61$$

$$(6, 5) \checkmark$$

$$2y^2 + 2y - 60 = 0$$

$$x = -6 + 1 = -5$$

$$y^2 + 1 - 30 = 0$$

$$(-5, -6)$$

$$(y - 5)(y + 6) = 0$$

$$y = 5, -6$$

HW p58 Q15

$$\text{Solve } 2t - 3s = 1 \Rightarrow t = \frac{3s+1}{2}$$

$$t^2 + ts - 4s^2 = 2$$

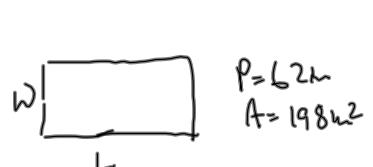
$$\left(\frac{3s+1}{2}\right)^2 + \left(\frac{3s+1}{2}\right)s - 4s^2 = 2$$

$$\frac{9s^2 + 6s + 1}{4} + \frac{3s^2 + s}{2} - 4s^2 = 2$$

$$9s^2 + 6s + 1 + 6s^2 + 2s - 16s^2 = 8$$

$$\begin{aligned} -1s^2 + 8s - 7 &= 0 \\ s^2 - 8s + 7 &= 0 \\ (s-1)(s-7) &= 0 \\ s = 1, 7 & \end{aligned} \quad \left| \begin{array}{l} t = \frac{3(1)+1}{2} = 2 \\ t = \frac{3(7)+1}{2} = 11 \end{array} \right.$$

p.59 Q3 and Q4



$$2w + 2L = 62 \quad \checkmark$$

$$Lw = 198 \quad \checkmark$$

$$w = \frac{198}{L}$$

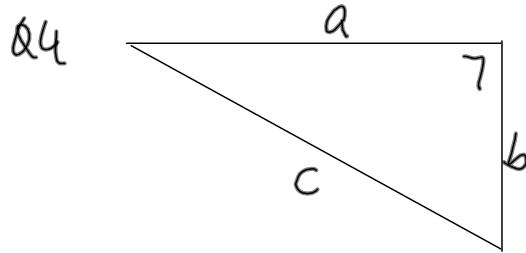
$$2\left(\frac{198}{L}\right) + 2L = 62 \quad \left| \begin{array}{l} w = \frac{198}{22} = 9 \\ w = \frac{198}{2} = 99 \end{array} \right.$$

$$396 + 2L^2 = 62L \quad \left| \begin{array}{l} w = \frac{198}{22} = 9 \\ w = \frac{198}{2} = 99 \end{array} \right.$$

$$L^2 - 31L + 198 = 0$$

$$(L-18)(L-11) = 0$$

$$L = 18, 11$$



Pythagoras Theorem

$$a^2 + b^2 = c^2$$

Consecutive nos

$$c = a+1, a = \underline{b+1}, c = \underline{b+2}$$

$P=?$

$$(b+1)^2 + b^2 = (b+2)^2$$

$$\cancel{b^2} + 2b + 1 + b^2 = \cancel{b^2} + 4b + 4$$

$$b^2 - 2b - 3 = 0$$

$$(b-3)(b+1) = 0$$

$$b=3, \cancel{b=-1} \rightarrow$$

$$b=3$$

$$a=4$$

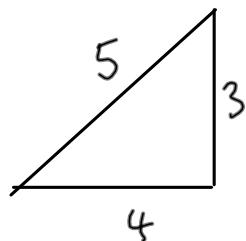
$$c=5$$

$$\hline$$

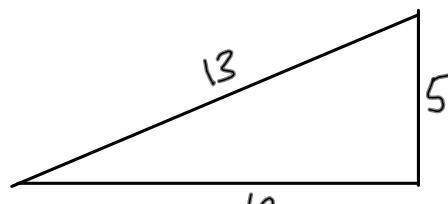
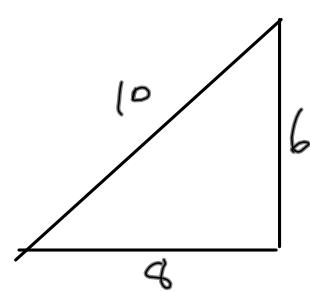
$$P=12$$

Pythagoras

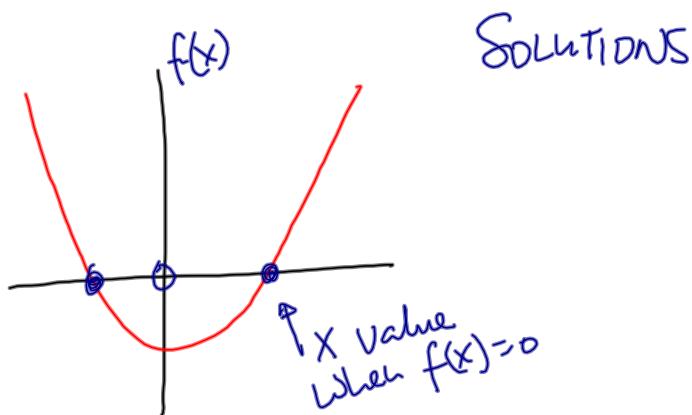
$$a^2 + b^2 = c^2$$



Examples of integer
Solutions to pythagoras
theorem



Roots of Quadratics



$$f(x) = x^2 + 2x + 1$$

SOLVE?

minus sum of roots Product of roots

$$(x+1)(x+1) = 0$$

$$\begin{array}{c|c} x+1=0 & x+1=0 \\ x=-1 & x=-1 \end{array}$$

Root or solution

$$f(x) = |x^2 - (r_1 + r_2)x + r_1 r_2$$

minus
 sum of roots Product
 of roots

$$X = r_1 \quad , \quad r_2$$

e.g., Roots are 7 and -5
 $\Rightarrow f(x) = |x^2 - 2x - 35$

Homework 18-10-2012

P.62 Q1 a) c) e)

Q3 i) ii) iii) iv)

Ex. 2.5 Q.1

$$(a) \quad x^2 + 9x + 4 = 0$$

Sum of Roots =

Product of Roots =

$$(c) \quad x^2 - 7x + 2 = 0$$

Sum of Roots =

Product of Roots =

$$(e) \quad 2x^2 - 7x + 1 = 0$$

Sum of Roots =

Product of Roots =

Ex 2.5 Find the quadratic equation that
Q3 has the following pairs of roots (r_1, r_2)

(i) $(4, 6)$

(ii) Find the quadratic equation that
 has the following pairs of roots (r_1, r_2)

$(2, -3)$

(iii) Find the quadratic equation that has the following pairs of roots (r_1, r_2)

$$(-5, -1)$$

(iv) Find the quadratic equation that has the following pairs of roots (r_1, r_2)

$$(\sqrt{5}, 4)$$