Question 1

An experiment consists of throwing two fair, standard, six-sided dice and noting the sum of the two numbers thrown. If the sum is 9 or greater it is recorded as a "win" (W). If the sum is 8 or less it is recorded as a "loss" (L).

(a) Complete the table below to show all possible outcomes of the experiment.

Die 2							
		1	2	3	4	5	6
Die 1	1		L				
	2						
	3						
	4						
	5						W
	6						

- (b) (i) Find the probability of a win on one throw of the two dice.
 - (ii) Find the probability that each of 3 successive throws of the two dice results in a loss. Give your answer correct to four decimal places.
- (c) The experiment is repeated until a total of 3 wins occur. Find the probability that the third win occurs on the tenth throw of the two dice. Give your answer correct to four decimal places.

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An experiment consists of throwing two fair, standard, six-sided dice and noting the sum of the two numbers thrown. If the sum is 9 or greater it is recorded as a "win" (W). If the sum is 8 or less it is recorded as a "loss" (L).

		Die 2							
		1	2	3	4	5	6		
Die 1	1	L	L	L	L	L	L		
	2	L	L	L	L	L	L		
	3	L	L	L	L	L	W		
	4	L	L	L	L	W	W		
	5	L	L	L	W	W	W		
	6	L	L	W	W	W	W		

(a) Complete the table below to show all possible outcomes of the experiment.

(b) (i) Find the probability of a win on one throw of the two dice.

$$P(W) = \frac{10}{36} = \frac{5}{18}$$

(ii) Find the probability that each of 3 successive throws of the two dice results in a loss. Give your answer correct to four decimal places.

$$P(L,L,L) = \left(\frac{13}{18}\right)^3 = 0.3767$$

(c) The experiment is repeated until a total of 3 wins occur. Find the probability that the third win occurs on the tenth throw of the two dice. Give your answer correct to four decimal places.

$$P(2 \text{ wins in } 9) = {9 \choose 2} \left(\frac{5}{18}\right)^2 \left(\frac{13}{18}\right)^7$$

$$P(3 \text{ wins, 3rd on 10th throw}) = {9 \choose 2} \left(\frac{5}{18}\right)^2 \left(\frac{13}{18}\right)^7 \left(\frac{5}{18}\right) = 0.0791$$

Section A

Question 1

(25 marks)

(a) Scale 10C (0, 4, 8, 10)

Low Partial Credit:

- At least one other correct entry
- Partially correct table with at least 5 correct totals or couples

High Partial Credit:

- Five or more correct entries including at least one other loss and one other win
- Table correctly completed with totals or couples but no indication of W or L

(b)(i)(ii) Scale 10C (0, 4, 8, 10)

Low Partial Credit:

- Favourable outcomes identified
- (i) correct only $(\frac{10}{36}, \frac{5}{18}, 0.27, 0.28, 0.3)$

High Partial Credit:

• (i) omitted or of no merit but (ii) $\left(\frac{13}{18}\right)^3$

(c) Scale 5C (0, 2, 4, 5)

Low Partial Credit:

- Relevant binomial formula with some substitution
- Identifies p^7 or $(1-p)^3$ or $(1-p)^2$ or 1-p
- Listing at least any two of the ten throws

High Partial Credit

Probability of two wins in nine throws