

Question 7

(40 marks)

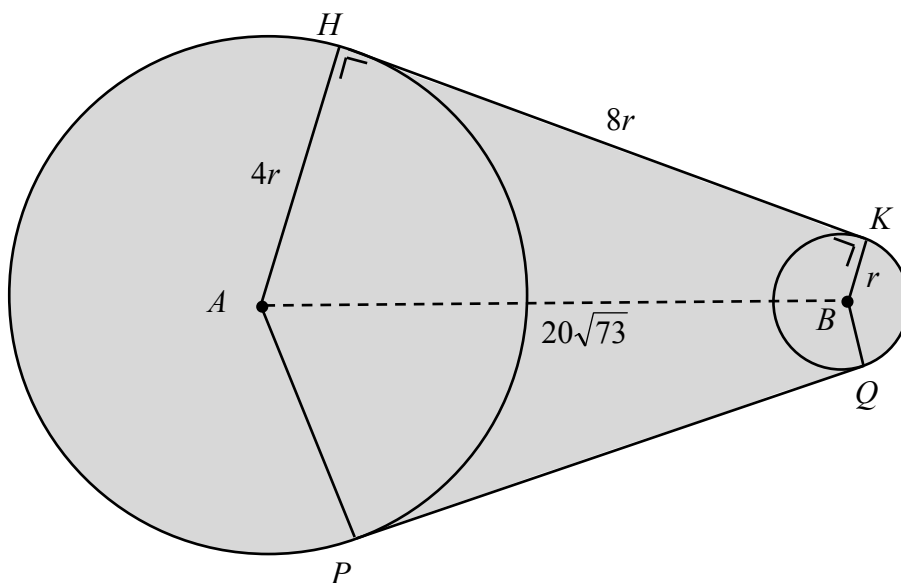
A flat machine part consists of two circular ends attached to a plate, as shown (diagram not to scale).

The sides of the plate, HK and PQ , are tangential to each circle.

The larger circle has centre A and radius $4r$ cm.

The smaller circle has centre B and radius r cm.

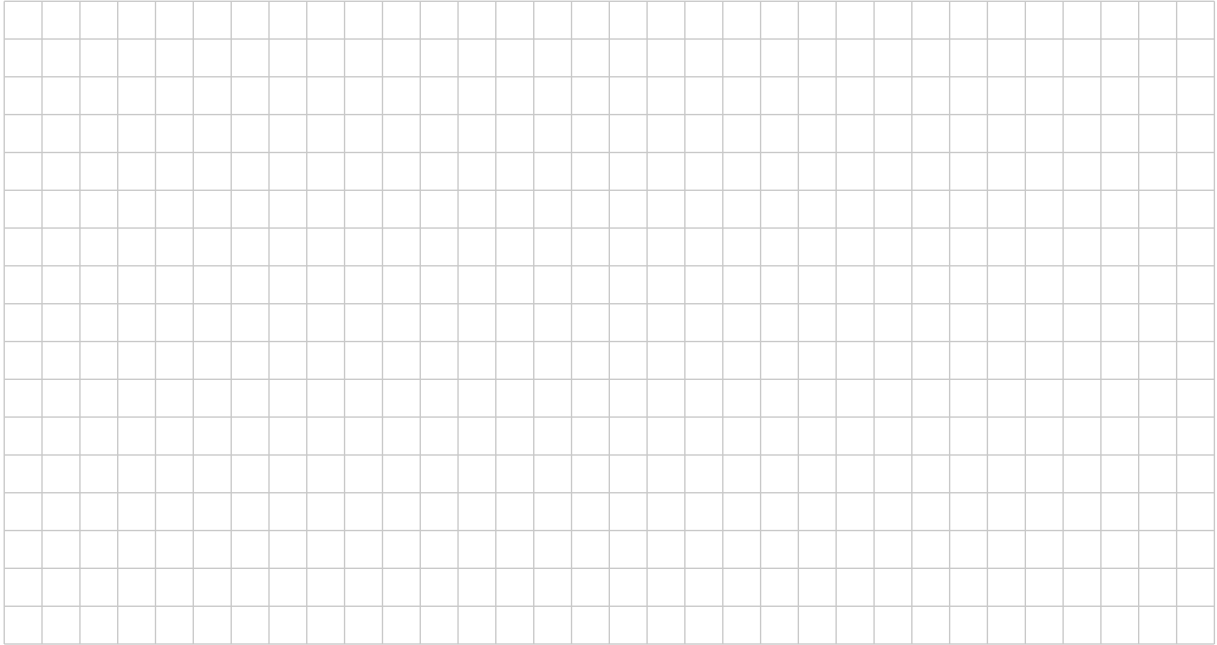
The length of $[HK]$ is $8r$ cm and $|AB| = 20\sqrt{73}$ cm.



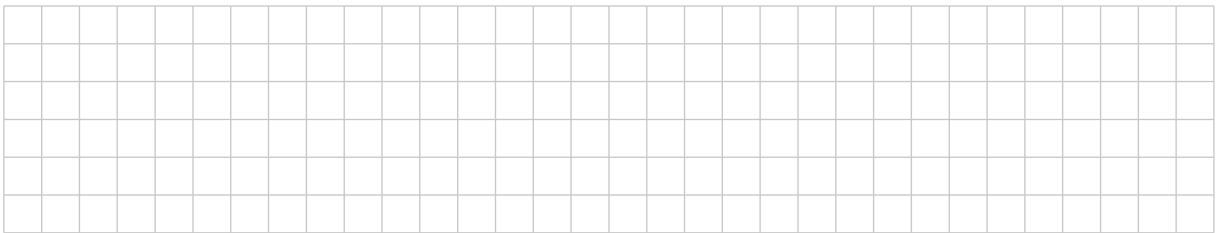
- (a) Find r , the radius of the smaller circle. (Hint: Draw $BT \parallel KH$, $T \in AH$.)



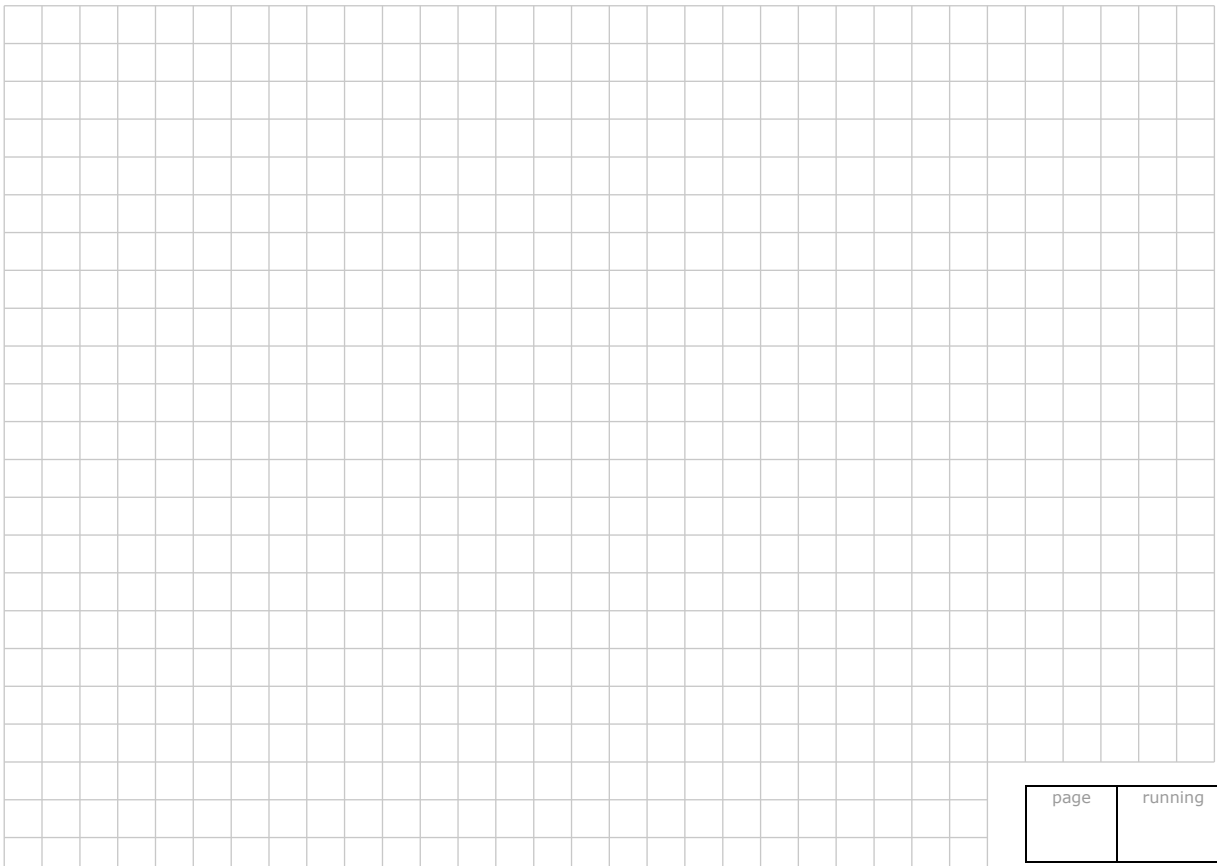
(b) Find the area of the quadrilateral $ABKH$.



(c) (i) Find $|\angle HAP|$, in degrees, correct to one decimal place.



(ii) Find the area of the machine part, correct to the nearest cm^2 .



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