

Question 3**(25 marks)**

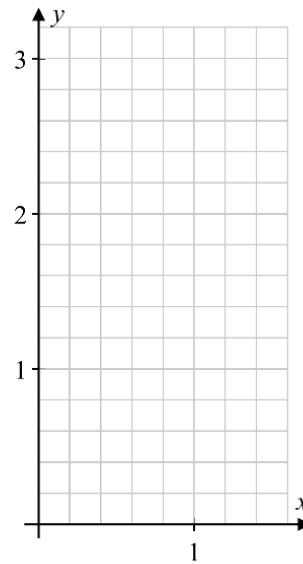
- (a) (i) $f(x) = \frac{2}{e^x}$ and $g(x) = e^x - 1$, where $x \in \mathbb{R}$.

Complete the table below. Write your values correct to two decimal places where necessary.

x	0	0.5	1	$\ln(4)$
$f(x) = \frac{2}{e^x}$				
$g(x) = e^x - 1$				

- (ii) In the grid on the right, use the table to draw the graphs of $f(x)$ and $g(x)$ in the domain $0 \leq x \leq \ln(4)$. Label each graph clearly.

- (iii) Use your graphs to estimate the value of x for which $f(x) = g(x)$.



- (b) Solve $f(x) = g(x)$ using algebra.

Q3	Model Solution – Continued	Marking Notes
(b)	$\frac{e^x - 1}{1} = \frac{2}{e^x}$ $e^{2x} - e^x = 2$ $(e^x)^2 - e^x - 2 = 0$ $(e^x - 2)(e^x + 1) = 0$ $e^x = 2 \text{ or } e^x = -1$ $x = \ln 2$ $\text{or } x = 0.693$ <p style="text-align: center;">Or</p> $(e^x)^2 - e^x - 2 = 0$ <p>Let $y = e^x \Rightarrow y^2 - y - 2 = 0$</p> $y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(-2)}}{2(1)}$ $= \frac{1 \pm \sqrt{1 + 8}}{2}$ $= \frac{1 \pm 3}{2}$ $\Rightarrow y = 2 \text{ or } y = -1 \text{ (not possible)}$ $y = e^x \Rightarrow e^x = 2$ $x = \ln 2 \text{ or } x = 0.693$	<p>Scale 10C (0, 3, 7, 10)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> substitution correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> correct factors of quadratic root formula correctly substituted $e^x = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(-2)}}{2(1)}$ <p>Note: oversimplification of equation (i.e. not treating as quadratic) merits Low Partial Credit at most</p> <p style="text-align: center;">Or</p> <p>Scale 10C (0, 3, 7, 10)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> substitution correct <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> root formula correctly substituted $y = \frac{-(-1) \pm \sqrt{(-1)^2 - 4(1)(-2)}}{2(1)}$ <p>Note: oversimplification of equation (i.e. not treating as quadratic) merits Low Partial Credit at most</p>