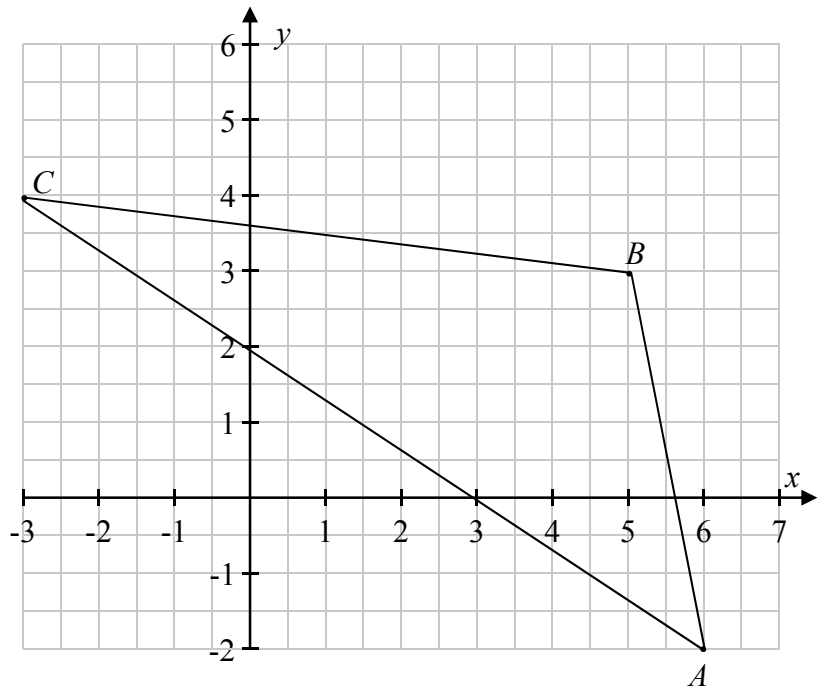


Question 1**(25 marks)**

The points $A(6, -2)$, $B(5, 3)$ and $C(-3, 4)$ are shown on the diagram.

- (a) Find the equation of the line through B which is perpendicular to AC .



- (b) Use your answer to part (a) above to find the co-ordinates of the orthocentre of the triangle ABC .

Q1	Model Solution – 25 Marks	Marking Notes
(a)	$\text{Slope } AC = -\frac{2}{3}$ $\text{perp. slope} = \frac{3}{2}$ $y - 3 = \frac{3}{2}(x - 5)$ $3x - 2y = 9$	<p>Scale 10C (0, 3, 7, 10)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • slope formula with some relevant substitution • $3 = 5m + c$ • $y - y_1 = m(x - x_1)$ with x_1 or y_1 or both substituted <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • perpendicular slope • equation of line through B parallel to AC
(b)	<p>Point of intersection of the altitudes</p> $\text{Slope } AB = \frac{3 + 2}{5 - 6} = -\frac{5}{1}$ $\text{perp. slope} = \frac{1}{5}$ $y - 4 = \frac{1}{5}(x + 3)$ $x - 5y + 23 = 0$ <p>Orthocentre: $3x - 2y = 9 \cap x - 5y = -23$</p> $\Rightarrow y = 6 \quad x = 7$ <p style="text-align: center;">(7, 6)</p> <p style="text-align: center;">or</p> <p>If BC chosen:</p> $\text{Slope } BC = \frac{3 - 4}{5 + 3} = -\frac{1}{8}$ $\text{perp. slope} = 8$ <p>Equation of altitude: $y + 2 = 8(x - 6)$ Equation: $8x - y = 50$ Orthocentre: $3x - 2y = 9 \cap 8x - y = 50$</p> $\Rightarrow y = 6 \quad x = 7$ <p style="text-align: center;">(7, 6)</p>	<p>Scale 15D (0, 4, 7, 11, 15)</p> <p><i>Low Partial Credit</i></p> <ul style="list-style-type: none"> • demonstration of understanding of orthocentre (e.g. mentions altitude) • slope formula with some relevant substitution • altitude from part (a) <p><i>Mid Partial Credit</i></p> <ul style="list-style-type: none"> • equation of an altitude other than (a) • some relevant substitution towards finding a second altitude and altitude from (a) • correct construction <p><i>High Partial Credit</i></p> <ul style="list-style-type: none"> • two correct altitudes • correct construction with orthocentre (7, 6)