Question 8

The height of the water in a port was measured over a period of time. The average height was found to be 1.6 m. The height measured in metres, h(t), was modelled using the function

$$h(t) = 1.6 + 1.5 \cos\left(\frac{\pi}{6}t\right)$$

where *t* represents the number of hours since the last recorded high tide and $\left(\frac{\pi}{6}t\right)$ is expressed in radians.

(a) Find the period and range of h(t).



(b) Find the maximum height of the water in the port.



(c) Find the rate at which the height of the water is changing when t = 2, correct to two decimal places. Explain your answer in the context of the question.



(d) (i) On a particular day the high tide occurred at midnight (i.e. t = 0). Use the function to complete the table and show the height, h(t), of the water between midnight and the following midnight.

			h(t) =	= 1.6 + 3	$1.5\cos\left(\frac{\pi}{6}\right)$	t)			
Time	Midnight	3 a.m.	6 a.m.	9 a.m.	12 noon	3 p.m.	6 p.m.	9 p.m.	Midnight
t (hours)	0	3							
h(t) (m)									

(ii) Sketch the graph of h(t) between midnight and the following midnight.



(e) Find, from your sketch, the difference in water height between low tide and high tide.

 (f) A fully loaded barge enters the port, unloads its cargo and departs some time later. The fully loaded barge requires a minimum water level of 2 m. When the barge is unloaded it only requires 1.5 m. Use your graph to estimate the **maximum** amount of time that the barge can spend in port, without resting on the sea-bed.

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