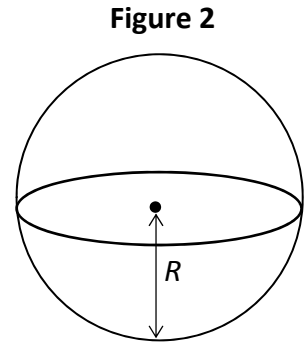
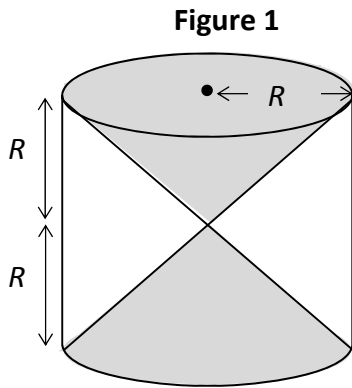


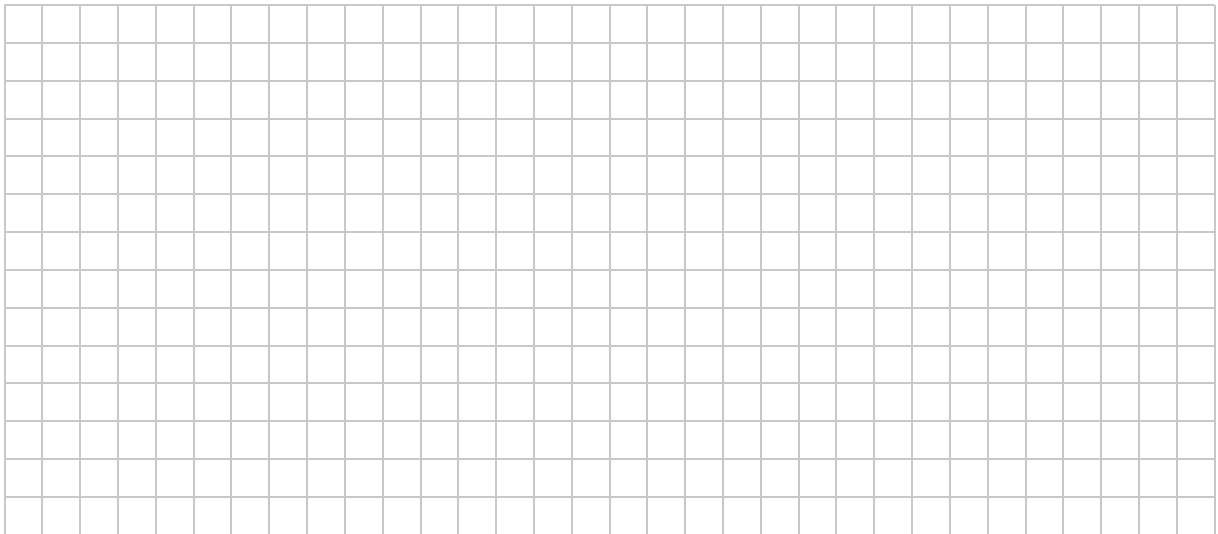
**Question 7**

**(40 marks)**

Two solid cones, each of radius  $R$  cm and height  $R$  cm are welded together at their vertices and placed in the smallest possible hollow cylinder, as shown in **Figure 1** below.



- (a)** Show that the capacity (volume) of the empty space in the cylinder is equal to the capacity of an empty sphere of radius  $R$  cm (**Figure 2**).





- (c) The mathematician Cavalieri discovered that, at the same depth, the volume of water in the available space in the cylinder is equal to the volume of water in the sphere.  
Use this discovery to find the volume of water in the sphere when the depth is 6 cm.  
Give your answer in terms of  $\pi$ .

