## Question 3

(a) Let $h(x)=\cos (2 x)$, where $x \in \mathbb{R}$.

A tangent is drawn to the graph of $h(x)$ at the point where $x=\frac{\pi}{3}$.
Find the angle that this tangent makes with the positive sense of the $x$-axis.

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(b) Find the average value of $h(x)$ over the interval $0 \leq x \leq \frac{\pi}{4}, x \in \mathbb{R}$. Give your answer in terms of $\pi$.


