## Question 2

(a) The circle $c$ has equation $x^{2}+y^{2}-4 x+2 y-4=0$. The point $A$ is the centre of the circle. The line $l$ is a tangent to $c$ at the point $T$, as shown in the diagram. The point $B(5,8)$ is on $l$. Find $|B T|$.


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(b) Two circles, $c_{1}$ and $c_{2}$, have their centres on the $x$-axis. Each circle has a radius of 5 units. The point $(1,4)$ lies on each circle. Find the equation of $c_{1}$ and the equation of $c_{2}$.


