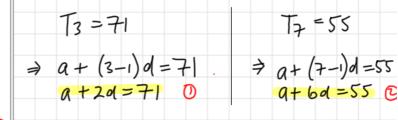
## **Revision Exercise (Core)**

- 1. Find the first four terms of these sequences given the *n*th term in each case:
  - (i)  $T_n = 3n + 4$
  - (ii)  $T_n = 6n 1$
  - (iii)  $T_n = 2^{n-1}$
  - (iv)  $T_n = (n+3)(n+4)$
  - (v)  $T_n = n^3 + 1$

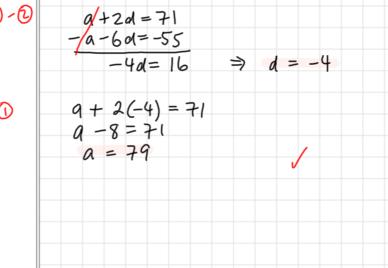
(1)	$T_1 = 3(1) + 4 = 7$ $T_2 = 3(2) + 4 = 10$ $T_3 = 3(3) + 4 = 13$ $T_4 = 3(4) + 4 = 16$	(iv) $T_1 = (1+3)(1+4) = 20$ $T_2 = (2+3)(2+4) = 30$ $T_3 = (3+3)(3+4) = 42$ $T_4 = (4+3)(4+4) = 56$
(ï)	$T_1 = 6(1) - 1 = 5$ $T_2 = 6(2) - 1 = 11$ $T_3 = 6(3) - 1 = 17$ $T_4 = 6(4) - 1 = 23$	(v) $T_1 = 1^3 + 1 = 2$ $T_2 = 2^3 + 1 = 9$ $T_3 = 3^3 + 1 = 28$ $T_4 = 4^3 + 1 = 65$
(iī)	$T_1 = 2^{1-1} = 2^{\circ} = 1$ $T_2 = 2^{2-1} = 2^{1} = 2$ $T_3 = 2^{3-1} = 2^{2} = 4$ $T_4 = 2^{4-1} = 2^3 = 8$	

**2.** The third term of an a<u>rithmetic sequence is</u> 71 and the seventh term is 55. Find the first term and the common difference.

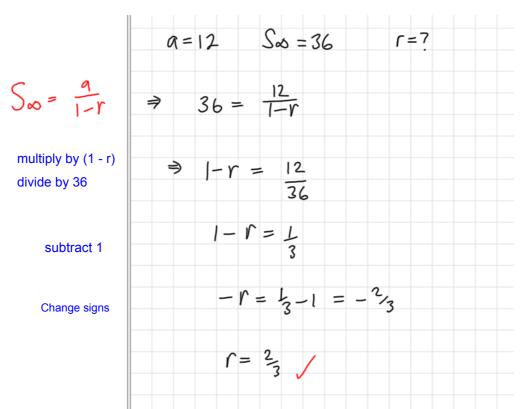
 $T_n = a + (n-1)d$ 



Solve (1) - (1)

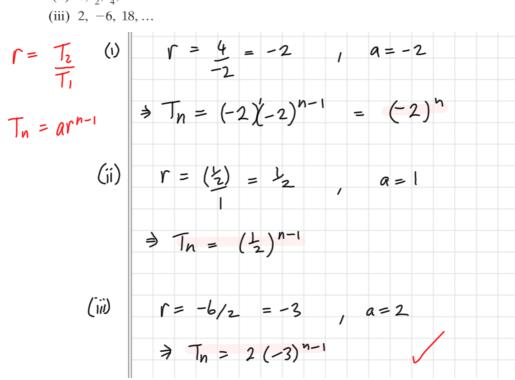


**3.** In a geometric series, the first term is 12 and the sum to infinity is 36. Find the common ratio.



**4.** Find the common ratio in each of the following geometric progressions and hence write an expression for  $T_n$ , the nth term.

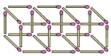
(ii) 
$$1, \frac{1}{2}, \frac{1}{4}, \dots$$



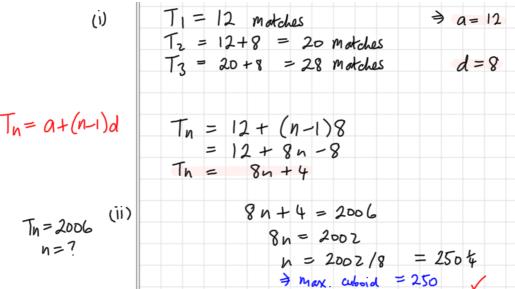
5. Using matchsticks, a series of cubes are made and joined as cuboids, as shown in the diagram.

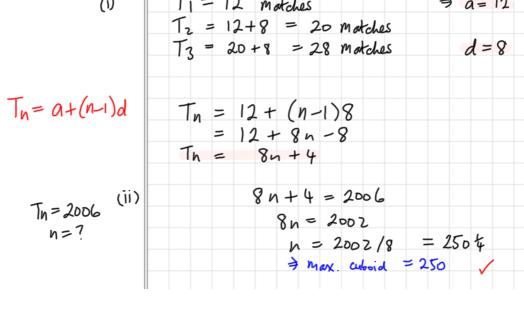


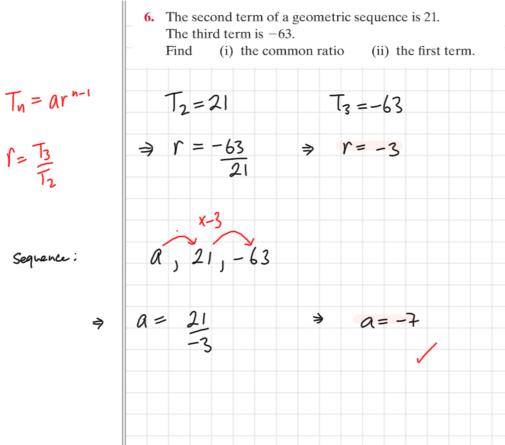




- (i) Determine the number of matchsticks needed for the *n*th cuboid.
- (ii) Determine the maximum number of cubes in the cuboid if there are 2006 matchsticks left for the construction.







7.  $\[ \epsilon 2000 \]$  is invested in a savings scheme which offers 2.5% compound interest. Explain how the expression  $A = \[ \epsilon 2000 (1.025)^{5} \]$  represents the value of the investment after 5 years.

$$A = amount \qquad r = rate$$

$$P = principle \qquad I = interest$$

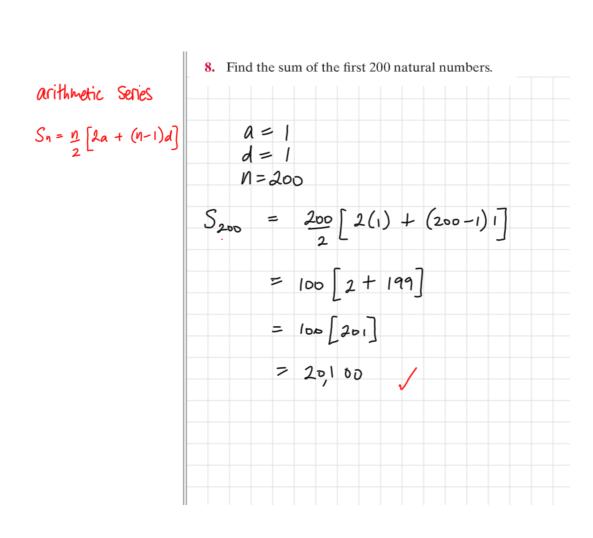
$$t = time \qquad p(r) = I$$

$$A_{1} = P + I \qquad = P + P(r) = P(1+r)$$

$$A_{2} = P_{2} + I = P(1+r) + P(1+r) r$$

$$= P(1+r) + P(1+r) r$$

$$= P(1+r)^{2} \quad etc...$$
This is a geometric sequence:
$$A = P(1+r)^{t}$$



- **9.** The fifth term of an arithmetic sequence is twice the second term. The two terms also differ by 9.
  - Find the sum of the first 10 terms of the sequence.

