

Exercise 5.3

1. Calculate the future value of 36 monthly instalments of €20.00 at an interest rate of 0.5% per month. What is the total interest earned on these savings?

$$A = P(1+i)^t$$

$$\text{geometric Series} = 20 \underset{T_{36}}{(1.005)^{36}} + 20 \underset{T_{35}}{(1.005)^{35}} + \dots + 20 \underset{T_1}{(1.005)^1}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$T_1 = a = 20(1.005)^1 = 20.1$$

$$r = 1.005 \quad (\text{Common Ratio})$$

$$n = 36$$

$$S_{36} = \frac{20.1(1 - 1.005^{36})}{1 - 1.005}$$

$$= \text{€}790.66$$

Example 3

What amount of money is needed now to provide a pension of €25 000 a year for 20 years, assuming an AER of 4%?

$$A = P(1+i)^t$$

$$\Rightarrow P = \frac{A}{(1+i)^t}$$

Geometric Series

$$\text{Total} = \frac{25000}{(1.04)^{20}} + \frac{25000}{(1.04)^{19}} + \dots + \frac{25000}{(1.04)^1}$$

T_{20} T_{19} T_1

$\times \frac{1}{1.04}$

$$a = T_1$$

$$a = 25000 / 1.04 = 24038.46$$

$$\text{Ratio: } r = \frac{T_2}{T_1}$$

$$r = \frac{1}{1.04}$$

$$S_n = \frac{a(1-r^n)}{1-r}$$

$$S_{20} = \frac{24038.46(1 - (\frac{1}{1.04})^{20})}{1 - (\frac{1}{1.04})}$$

$$= \text{€} 339,758.16$$